

# Revisiting the image source model: Towards geometry-based modeling of agent-to-agent channels

**Josef Kulmer and Klaus Witrisal**

**Graz, University of Technology**

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# Geometry-based multipath propagation

## Motivation

- indoor positioning requires infrastructure, e.g. anchor nodes
  - multipath propagation contains position-related information
- omit anchors and utilize multipath propagation

## Challenge

- modeling of multipath propagation agent-to-agent channels
- widely used multipath models assume static anchors

## Contribution

- revisit multipath propagation model
- rephrase propagation models to deal with cooperative agent nodes
- analyze covered information in multipath delays

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# Multipath assisted indoor localization

Agent node  $m$  at  $\mathbf{p}^{(m)} \in \mathbb{R}^2$  locates its position using multipath channel propagation to anchor  $m'$  at known position  $\mathbf{p}^{(m')} \in \mathbb{R}^2$ .

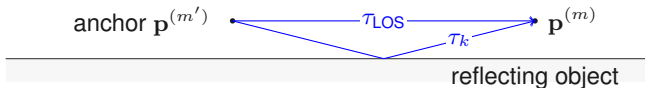
- Setup



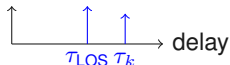
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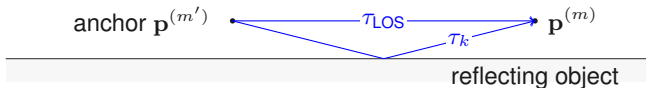
- Measurement: multipath components (MPC) contained in channel impulse response



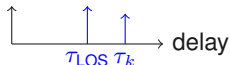
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- Setup



- Measurement: multipath components (MPC) contained in channel impulse response



- Objective: estimate agent position  $\mathbf{p}^{(m)}$  using MPCs  $\tau_{\text{LOS}}, \tau_k$ .



# Multipath assisted indoor localization

## Modeling of specular reflection $\tau_k$

- (optical) ray model<sup>1</sup>
- neglect propagation effects like diffraction or penetration

## Prominent solution for non-cooperative setup

- image source model<sup>2</sup>

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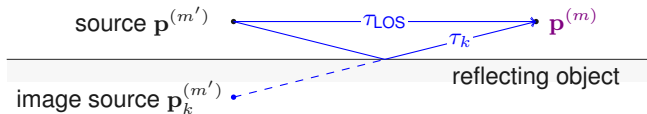
<sup>1</sup> Kuttruff: Room Acoustics. Elsevier. 1973

<sup>2</sup> J Kulmer, E Leitinger, P Meissner, S Hinteregger, K Witrissal: "Cooperative indoor localization using multipath channel information", ICL-GNSS 2016

# Image source model

Modeling of specular reflection  $\tau_k$  using image source model

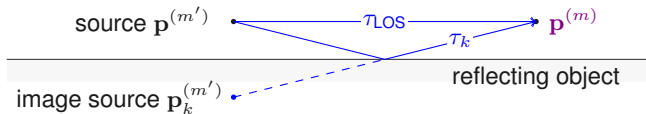
- define anchor as *source*
- obtain *image sources* at reflective objects



# Image source model

## Modeling of specular reflection $\tau_k$ using image source model

- define anchor as *source*
- obtain *image sources* at reflective objects



## MPC delays result as geometric distances

- measurement model:  $\tau_{\text{LOS}} = \|\mathbf{p}^{(m')} - \mathbf{p}^{(m)}\|/c$   
 $\tau_k = \|\mathbf{p}_k^{(m')} - \mathbf{p}^{(m)}\|/c$
- estimate agent position  $\mathbf{p}^{(m)}$  using  $\tau_{\text{LOS}}$  and  $\tau_k$

# Image source model

## Limitations

- one node (source) needs to be static
  - appropriate for non-cooperative setup
  - in cooperative setup there is no static anchor
- dependencies among MPCs are not considered
  - single reflective object is bounced by several MPCs
  - impact of object parameters on MPC delays

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Proposal<sup>3</sup>: relate MPC delays to reflective objects rather than to static image sources

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# Proposed geometry model

Incorporate parameters of reflective objects in measurement function

- image source model: MPCs are related to image sources

$$\tau_k = \|\mathbf{p}_k^{(m')} - \mathbf{p}^{(m)}\|/c$$

- proposal: relate MPCs to reflective objects

$$\tau_k = \|d(\mathbf{p}^{(m)}, \mathbf{p}^{(m')}, \{\text{reflective object parameters}\})\|/c$$

## Benefits

- single equation for each MPC
- consider mutual dependencies of MPCs

# Proposed geometry model

## Measurement function

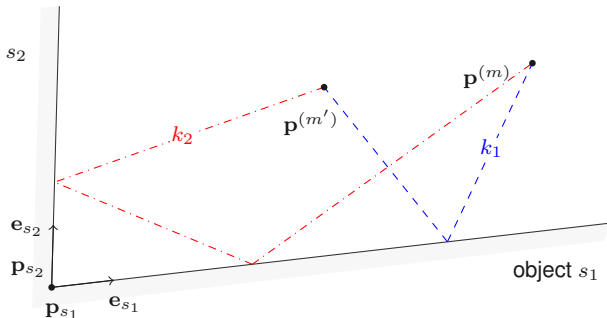
$$\tau_k = \|d(\mathbf{p}^{(m)}, \mathbf{p}^{(m')}, \{\text{reflective object parameters}\})\|/c$$

## Insights

- represent reflective objects by one point on its surface  $\mathbf{p}_s$  and by its orientation  $\mathbf{e}_s$
- $d(\mathbf{p}^{(m)}, \mathbf{p}^{(m')}, \{\mathbf{p}_s, \mathbf{e}_s\})$ 
  - affine transformation of  $\mathbf{p}^{(m)}, \mathbf{p}^{(m')}$  and  $\{\mathbf{p}_s\}$
  - non-linear transformation of  $\{\mathbf{e}_s\}$
- how are vectors  $\mathbf{p}^{(m)}, \mathbf{p}^{(m')}$  and  $\{\mathbf{p}_s\}$  affected by the measured scalars  $\tau_{\text{LOS}}$  and  $\tau_k$ ?

# Covered information in MPCs

Illustration of single bounce  $k_1$  and double bounce reflection  $k_2$

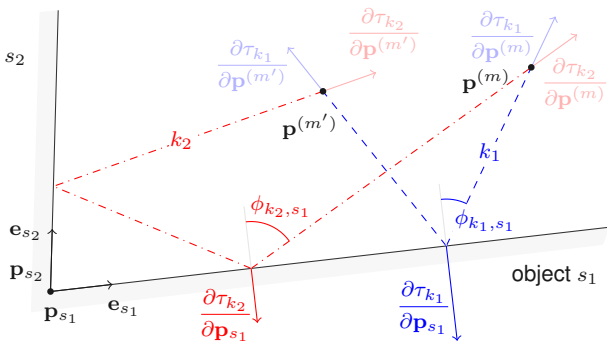






# Covered information of reflective object locations

$$\|\partial\tau_k/\partial\mathbf{p}_s\| = -2 \cos(\phi_{k,s})\dot{\mathbf{e}}_s/c$$



# Insights

## Contained information in MPCs regarding agent positions

- position information in direction of arriving / departing MPCs
- independent of arrangement of agents
- change of  $|\Delta\tau| = 1$  translates to  $\|\Delta\mathbf{p}^{(m)}\|/c = 1$

## Information regarding locations of reflective objects

- obtained information perpendicular to object orientation
- arrangement of agents determines arriving angle
- change of  $|\Delta\tau| = 1$  yields (up to) doubled sensitivity  $\|\Delta\mathbf{p}_s\|/c = 2$

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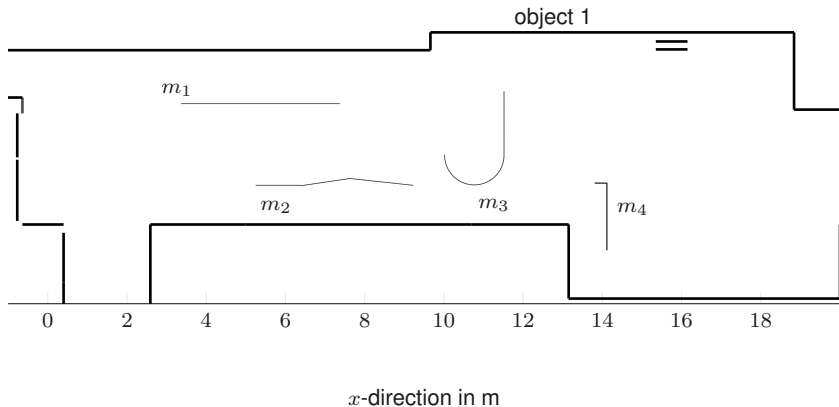
**MPC delays are more sensitive to object locations than agent positions**

# Application

Employ proposed geometry model for multipath assisted indoor tracking using real data

## Setup

- four cooperative agents  $m_1 \dots m_4$  move on trajectories of  $n \in \{1 \dots 200\}$  steps in a hallway
- at each step  $n$ , agents perform UWB measurements with an Ilimsense Channel Sounder
- bandwidth 1 GHz at center frequency of 7 GHz
- no information from an anchor node, position information entirely captured from MPCs



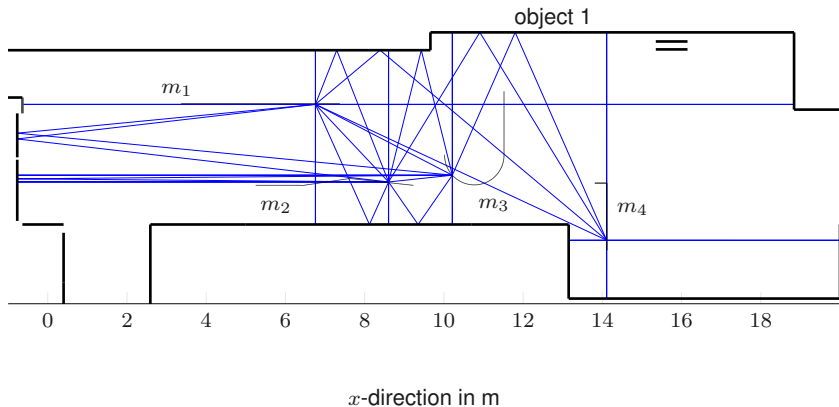
- consider objects with size  $> 25$  cm (walls, windows, doors)

# Application

## Algorithm

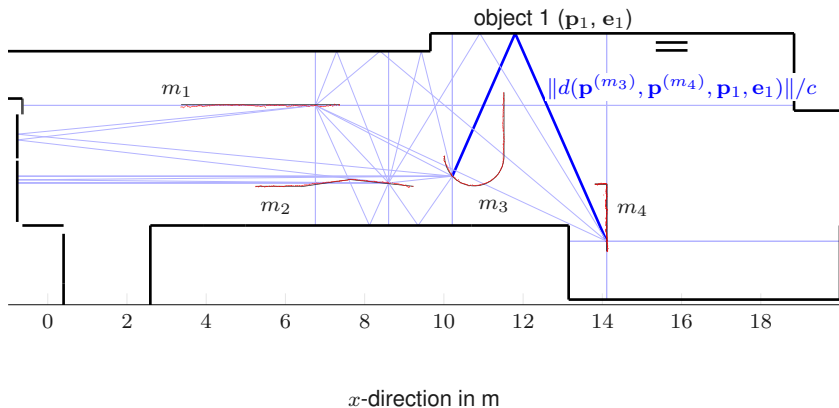
- estimation of MPC parameters  $\{\tau_k^{(m',m)}\}$
- Kalman Filter to recursively update position estimates  $\mathbf{p}_n^{(m_1)} \dots \mathbf{p}_n^{(m_4)}$  contained in state vector  $\mathbf{x}_n$  using MPC delays  $\{\tau_k\}$ 
  - linear motion model  $\mathbf{x}_n = f(\mathbf{x}_{n-1}) + \text{noise}$
  - measurement model

$$\begin{bmatrix} \tau_1^{(m_1, m_2)} \\ \tau_1^{(m_1, m_3)} \\ \dots \end{bmatrix} = \begin{bmatrix} \|d(\mathbf{p}_n^{(m_1)}, \mathbf{p}_n^{(m_2)}, \cdot, \cdot)\|/c \\ \|d(\mathbf{p}_n^{(m_1)}, \mathbf{p}_n^{(m_3)}, \cdot, \cdot)\|/c \\ \dots \end{bmatrix} + \text{noise}$$



- multipath propagation at step  $n = 30$  in blue

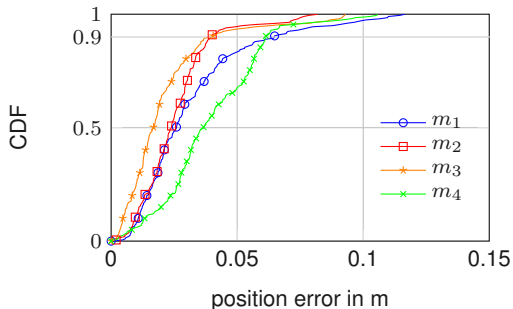




- illustration of gained information from specular reflection between  $m_3$  and  $m_4$

# Application

## Results



- position error in sub-meter range
- increased performance of  $m_2$  and  $m_3$

# Summary

## Summary

- revisit geometric multipath models for agent-to-agent channels
- analyzed impact of agent position and reflective object locations on multipath propagation
- utilized multipath model for tracking of cooperative agents without using information from anchors

## Future work

- expansion of geometry model to point scatters and complex shapes
- investigations on impact of reflector orientation